



► TECHNOLOGIE POLYMERE & KOMPOSITE

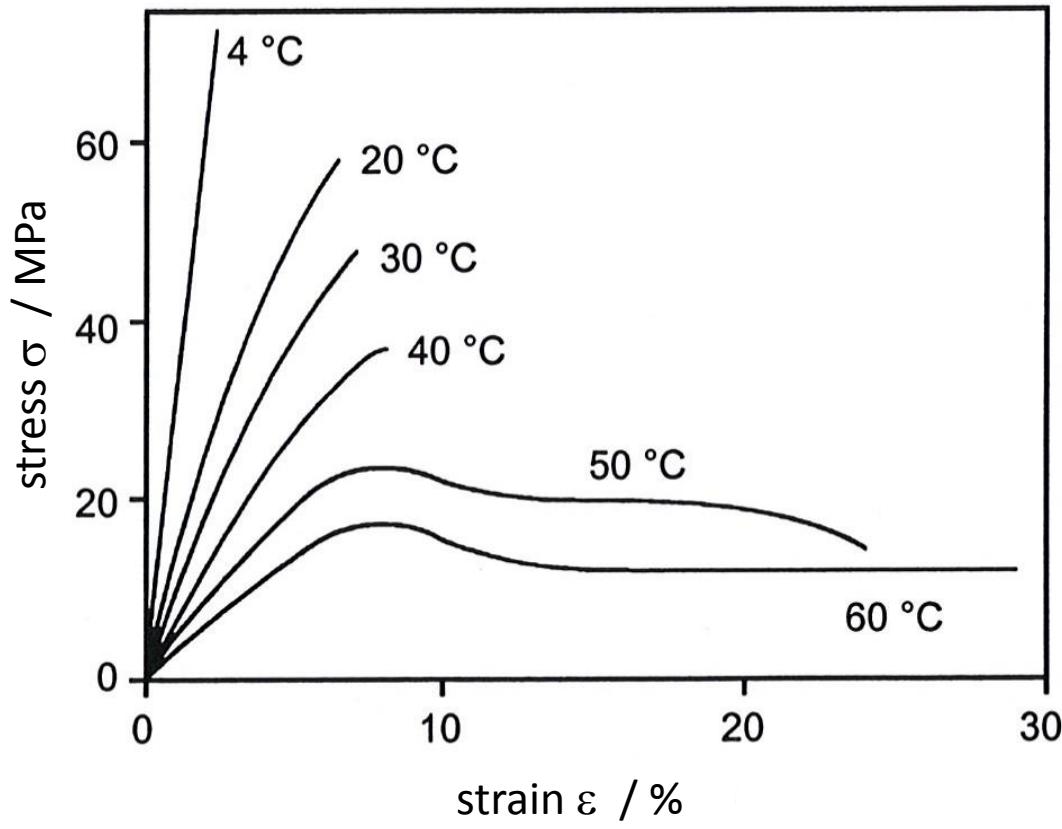
MC07, UdS WS 2019/2020

Chapter 5: Visco-elastic behaviour

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► Temperature dependence in stress strain behaviour

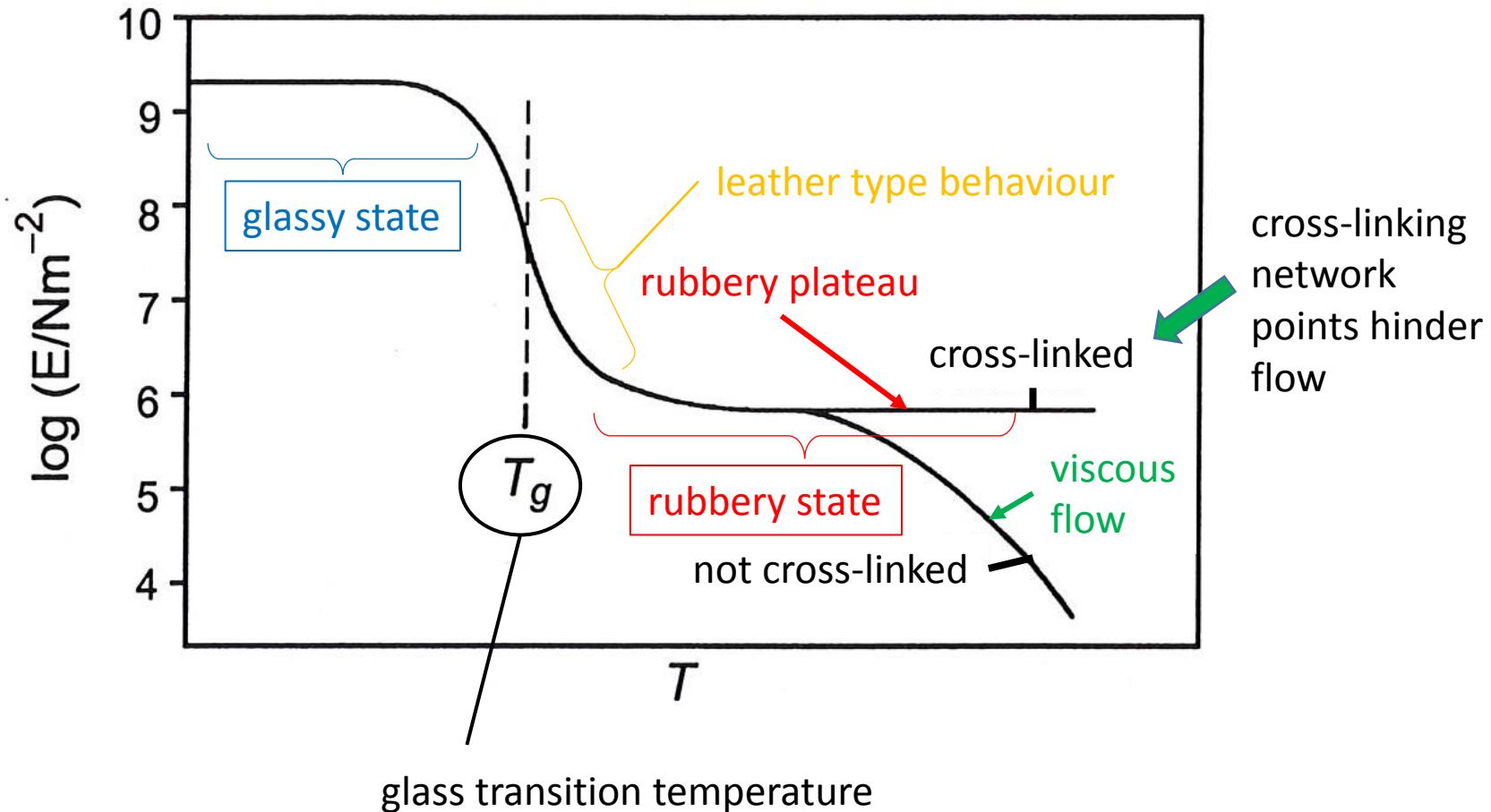
example: PMMA (polymethylmethacrylate)



! polymers are visco-elastic materials → time temperature equivalence !

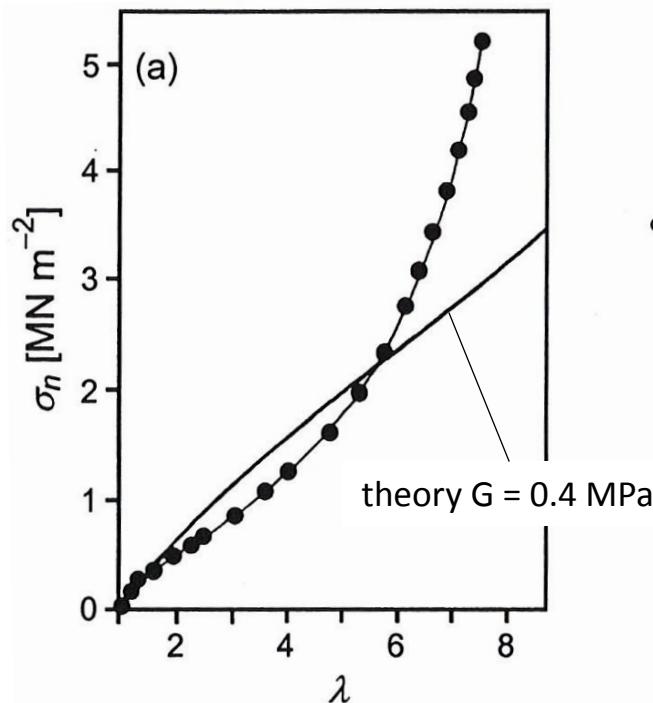
Elastic modulus vs temperature

general behaviour of thermoplastic materials and influence of cross-linking

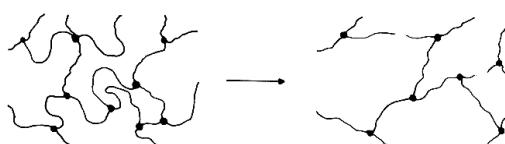
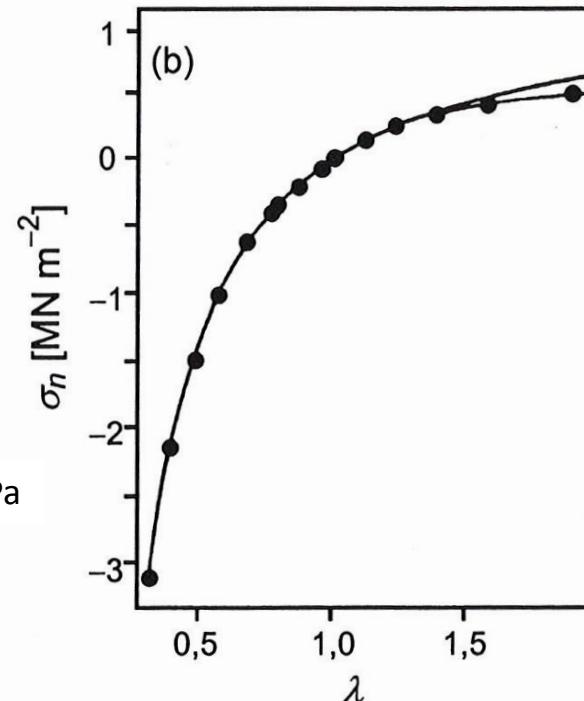


► Stress strain for elastomers (elastic behaviour)

tensile



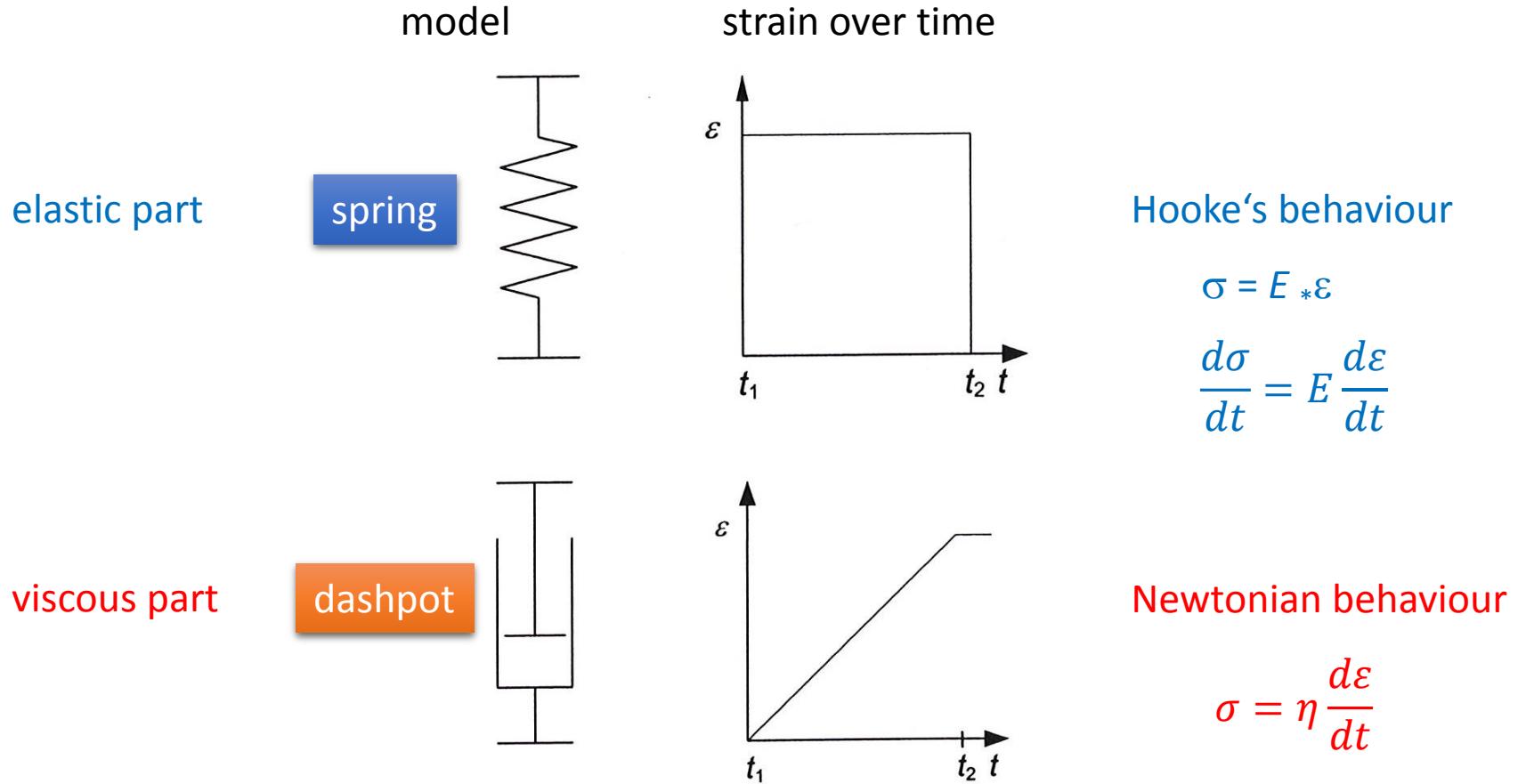
compression



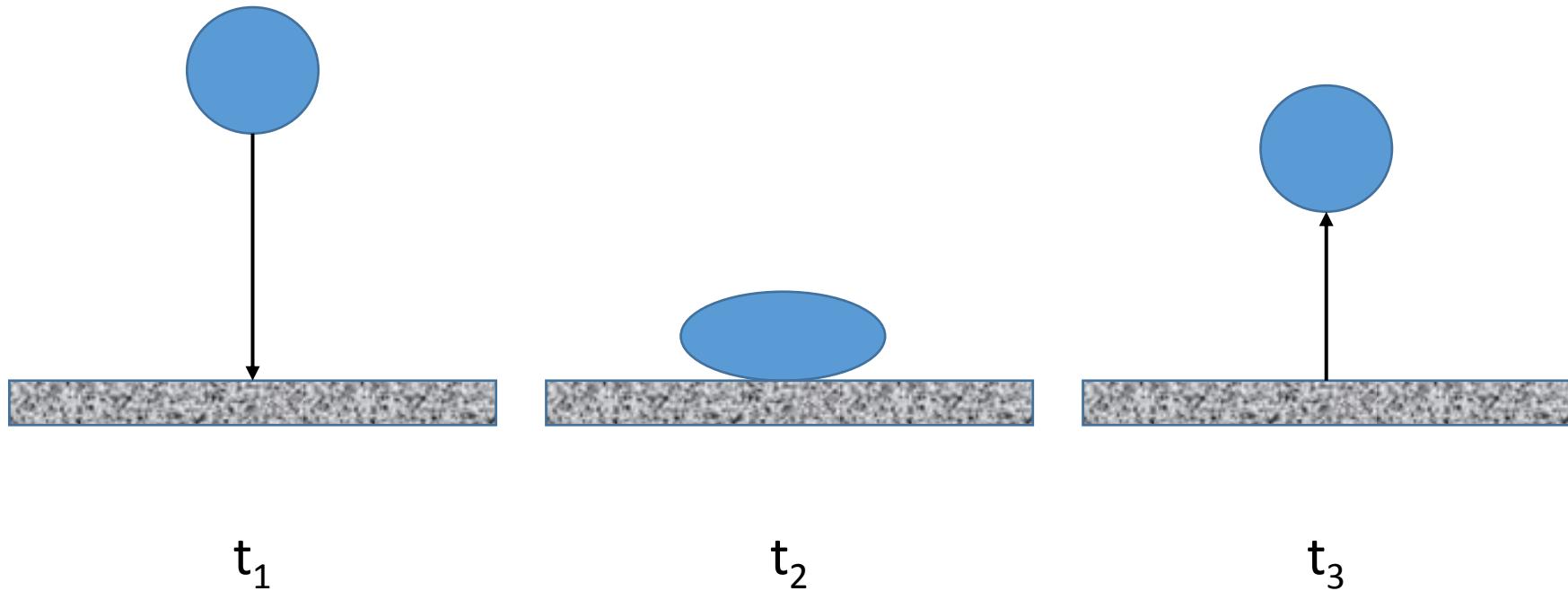
e.g. tensile mode:

- stress increases for higher strain
- covalent network points hinder slippage between chains
- elastic energy can be restored when strain is released
- entropy elasticity

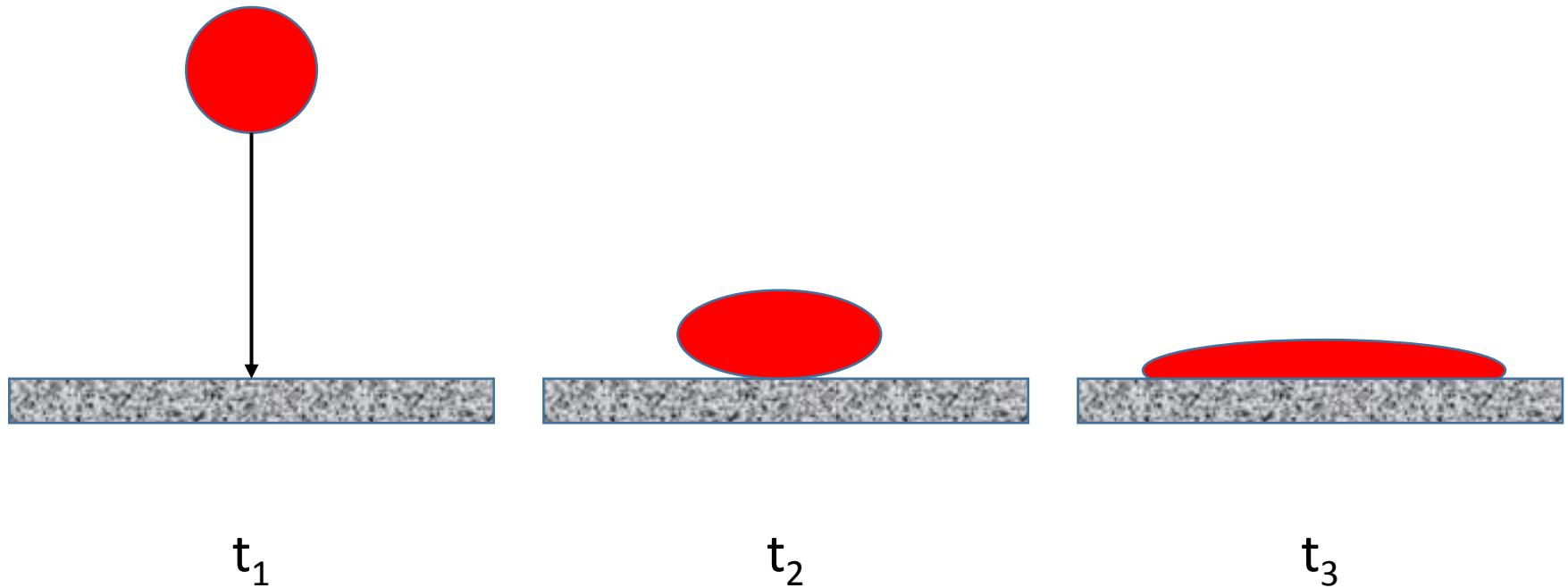
► Models to describe molecular mechanisms in polymers



► Elastic behaviour



► Viscous behaviour



► Extreme visco-elastic behaviour: „silly putty“



- non-newtonian viscosity

- long loading times
 - viscous flow (creep)

- short loading times
 - elastic behaviour

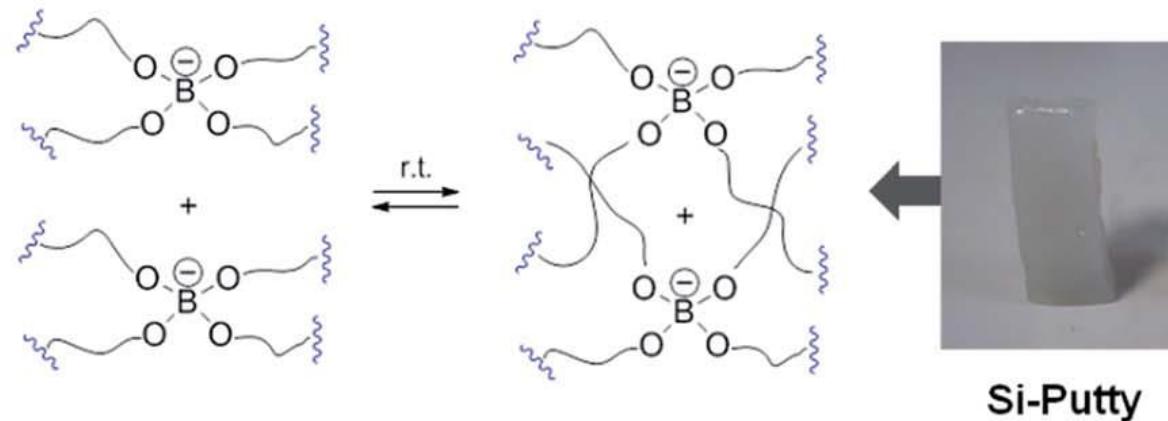
- extrem short loading times
 - brittle behaviour



► Extreme visco-elastic behaviour

- mixture of:

- 65% HO-PDMS-OH terminated with $B(OH)_3$
- 17% silica
- 9% Thixatrol ST (castor oil or derivative)
- 4% PDMS
- 1% decamethyl cyclopentasiloxane
- 1% glycerine
- 1% TiO_2



► Creep behaviour

- strain ε is dependent on:

- stress σ
- temperature T
- time t

$$\varepsilon = f(\sigma, T, t)$$

- time and temperature dependent deformation processes are called **creep** behaviour

Creep behaviour



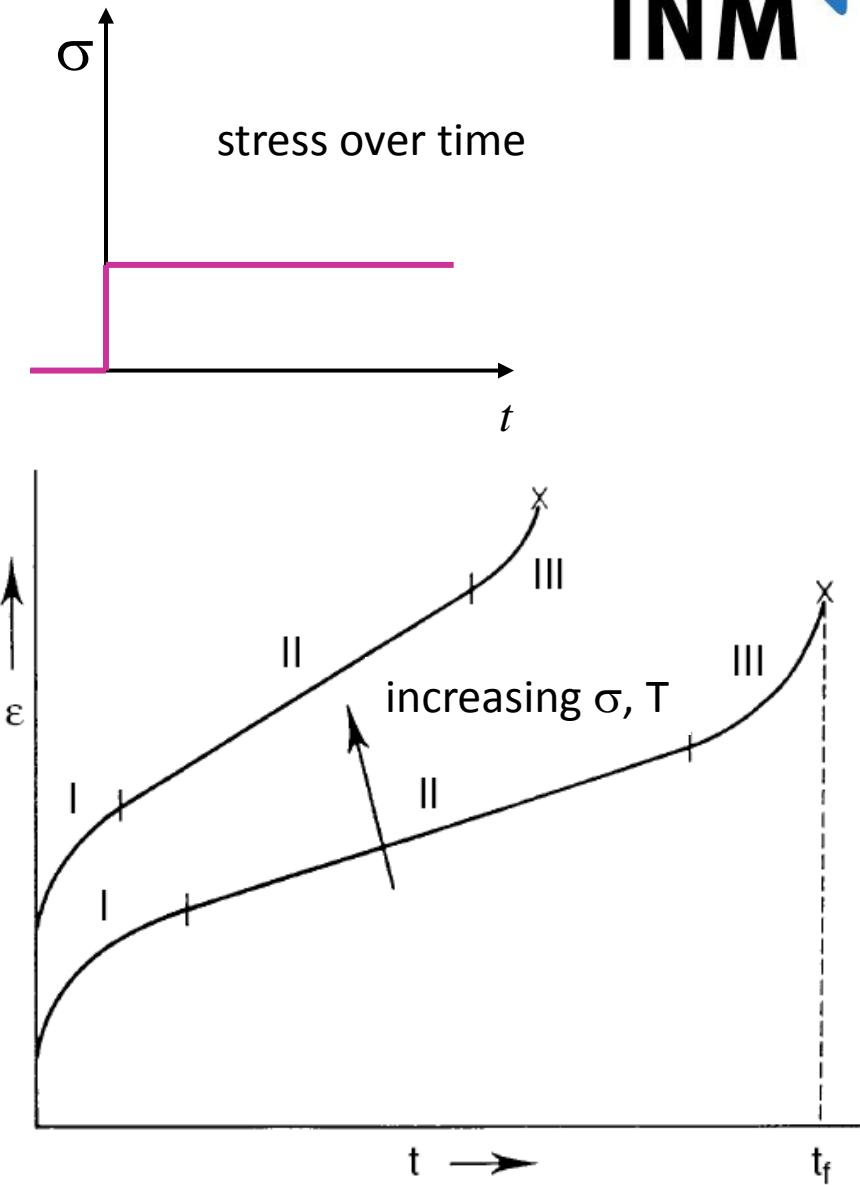
primary creep (I)

- creep velocity can decrease because of solidification mechanisms
- $$\varepsilon_I = \alpha \log t$$

stationary creep (II)

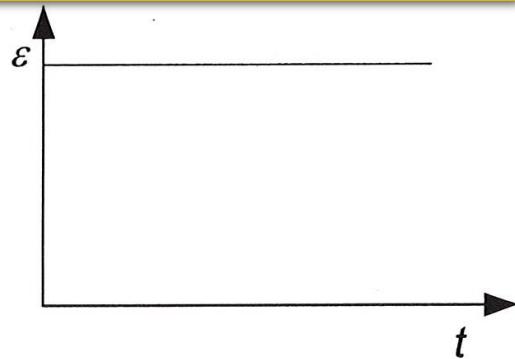
- dynamic equilibrium between weakening and re-solidification
- $$\varepsilon_{II} = \alpha \log t$$

tertiary creep (III)



The visco-elastic response under constant strain and constant stress

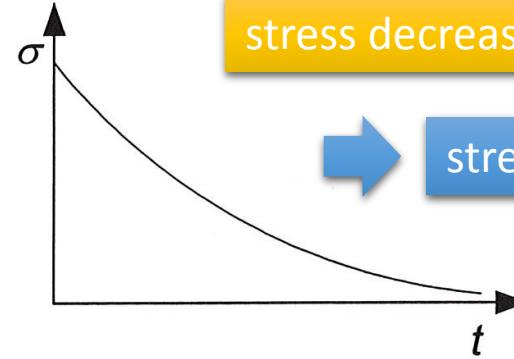
constant strain over time



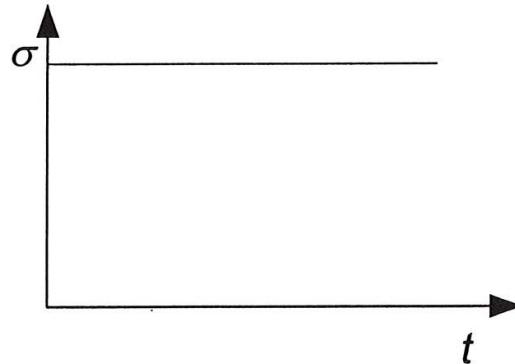
stress decreases in sample



stress relaxation



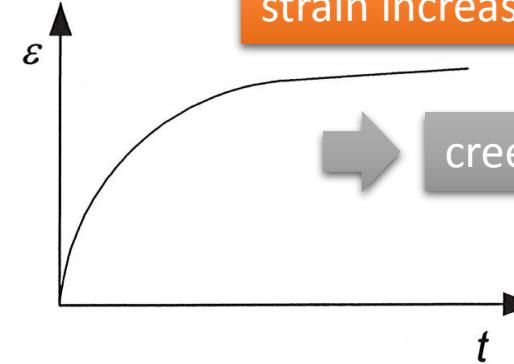
constant stress over time



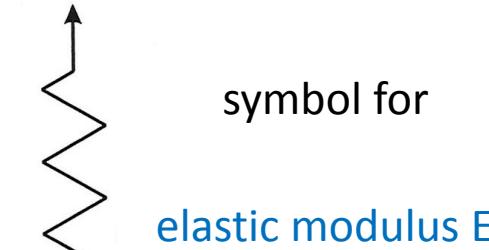
strain increases in sample



creep behaviour

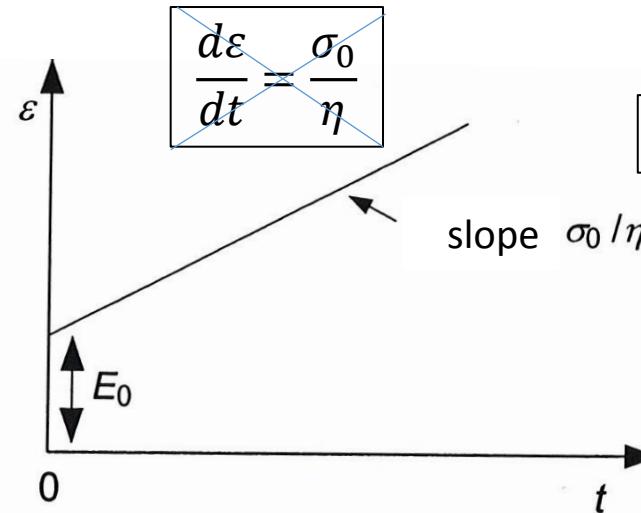


► Maxwell model: Spring and dash-pot in series



$$\frac{d\varepsilon}{dt} = \frac{1}{E} \frac{d\sigma}{dt} + \frac{\sigma}{\eta}$$

measurement at constant stress



Newtownian flow

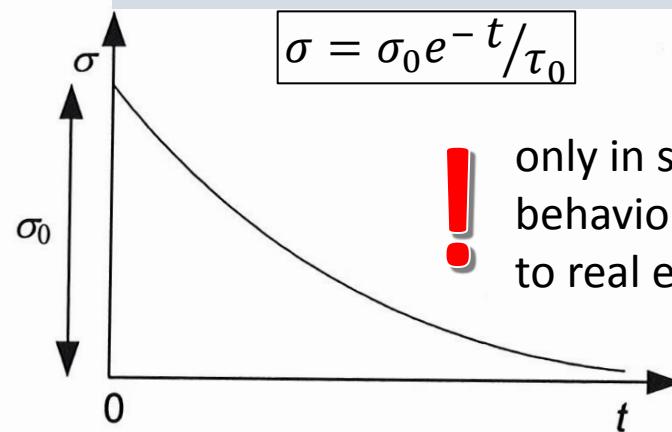


not suitable for
visco-elastic
behaviour

measurement at constant strain

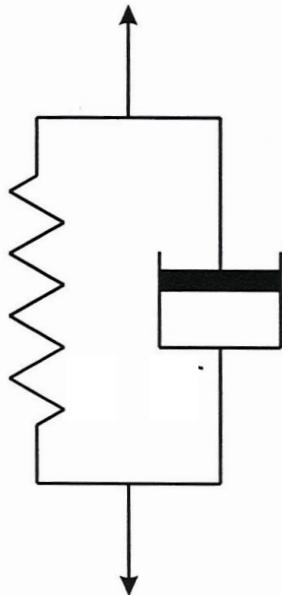
$$\sigma = \sigma_0 e^{-t/\tau_0}$$

stress relaxation

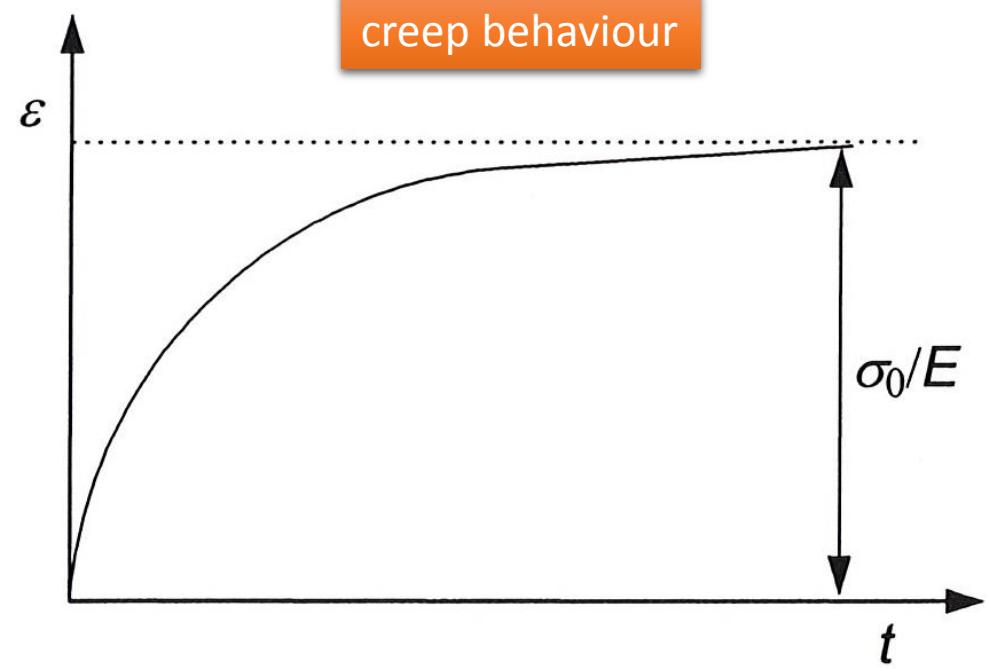


only in stress relaxation
behaviour Maxwell model fits
to real experiments

Kelvin-Voigt model: Spring and dash-pot in parallel



$$\sigma = E\varepsilon + \eta \frac{d\varepsilon}{dt} \quad \text{and} \quad \frac{d\varepsilon}{dt} = \frac{\sigma}{\eta} - \frac{E\varepsilon}{\eta}$$



measurement at constant stress:

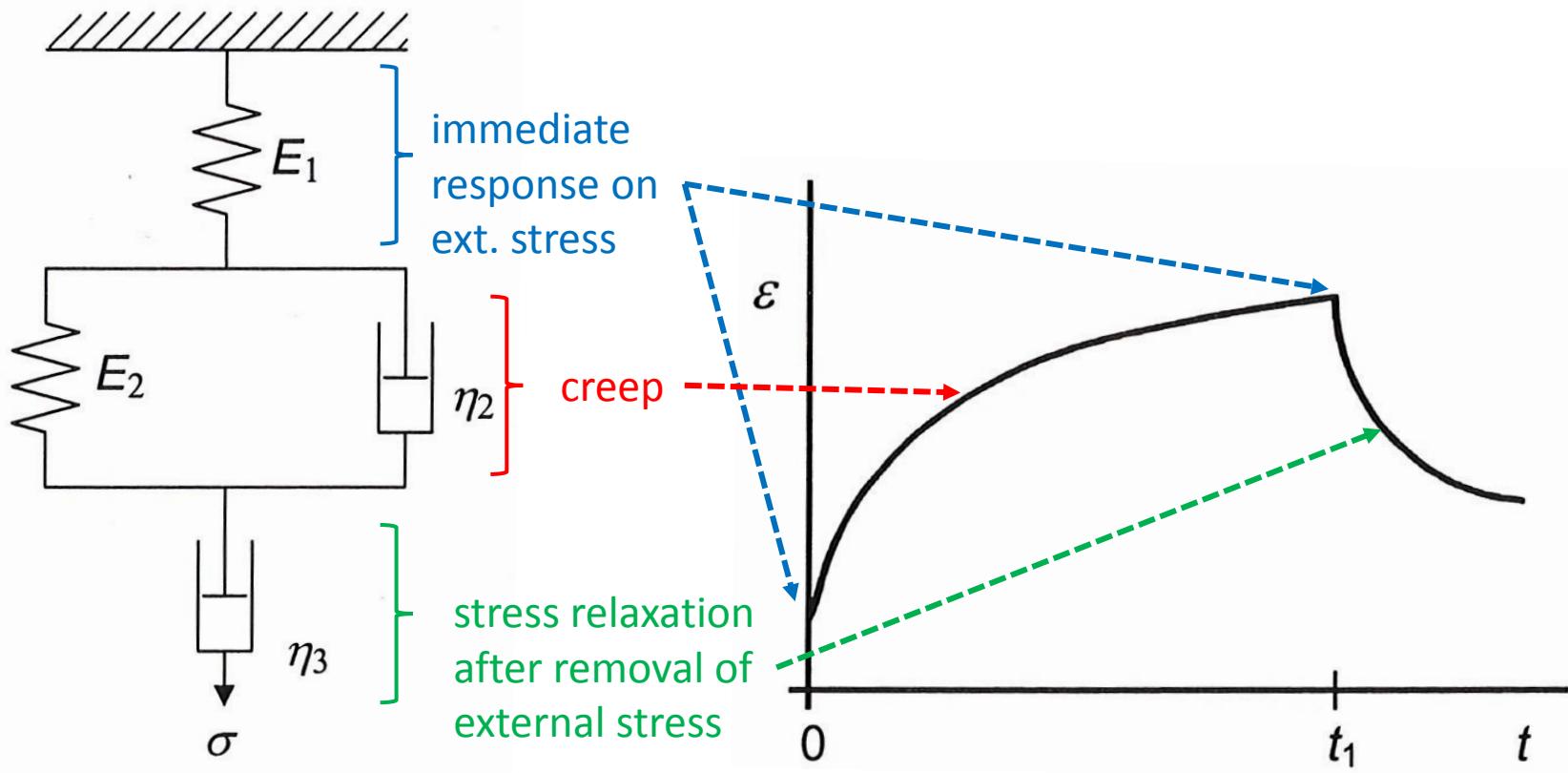
$$\varepsilon = \frac{\sigma_0}{E} \left[1 - e^{-t/\tau_0} \right] \quad \tau_0: \text{relaxation time}$$



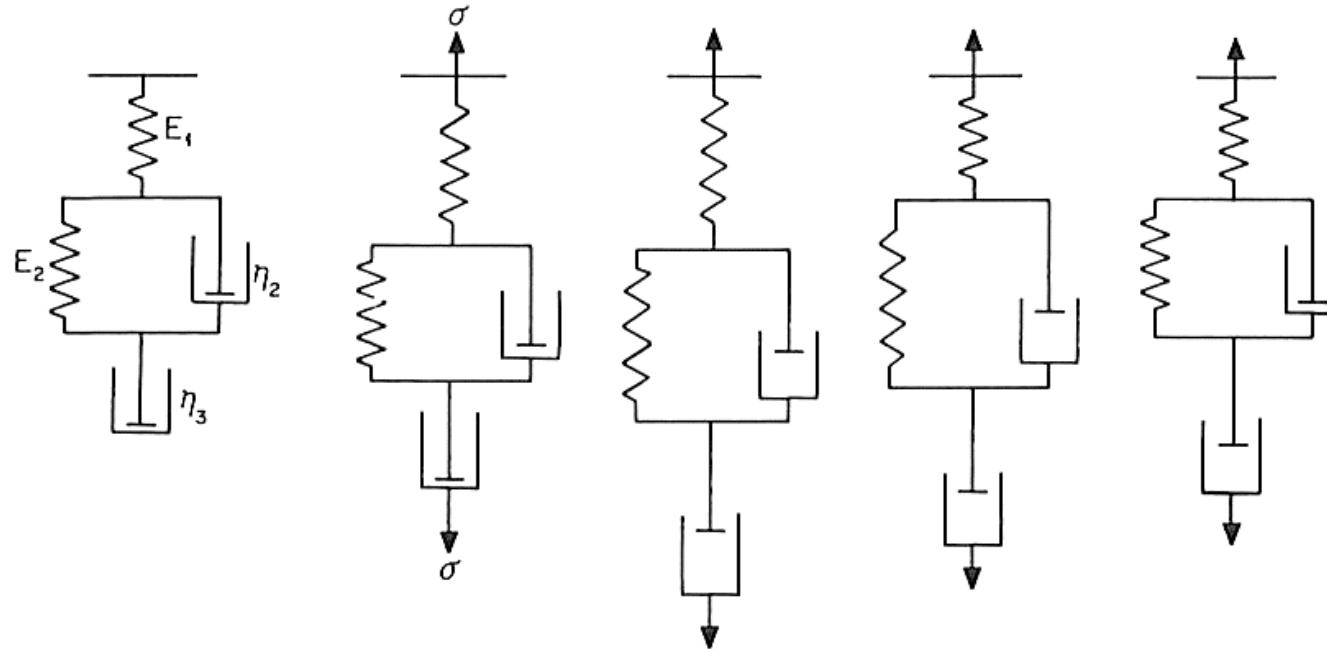
Kelvin-Voigt model fits well to creep behaviour observed in real experiments

▶ Combinations of serial and parallel elements

improvement of models by combination of
Maxwell and Kelvin-Voigt elements: **Burgers model**

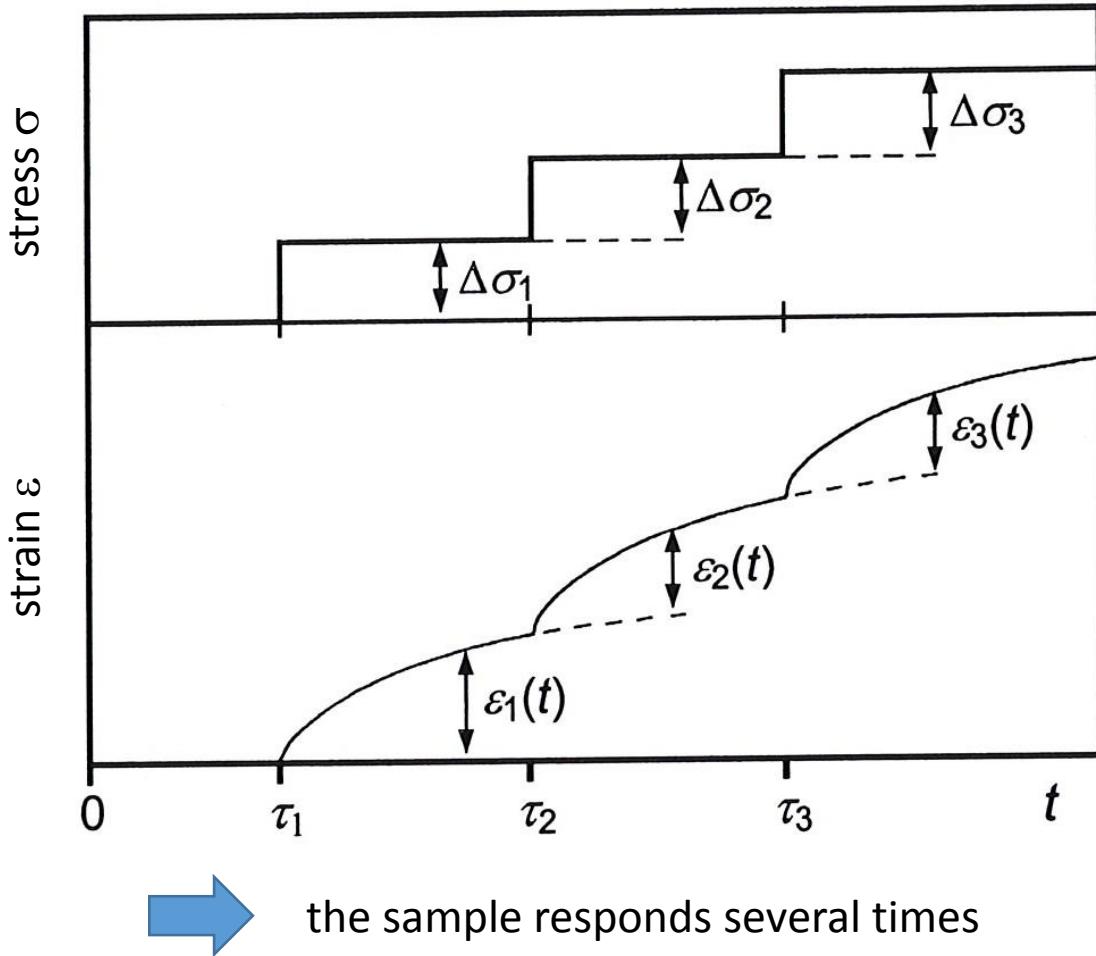


► Use of mechanical models to describe creep of polymers



Boltzmann's superposition principle I

strain of a visco-elastic material after several tensile deformations



externally applied stress
 σ (stepwise increase)

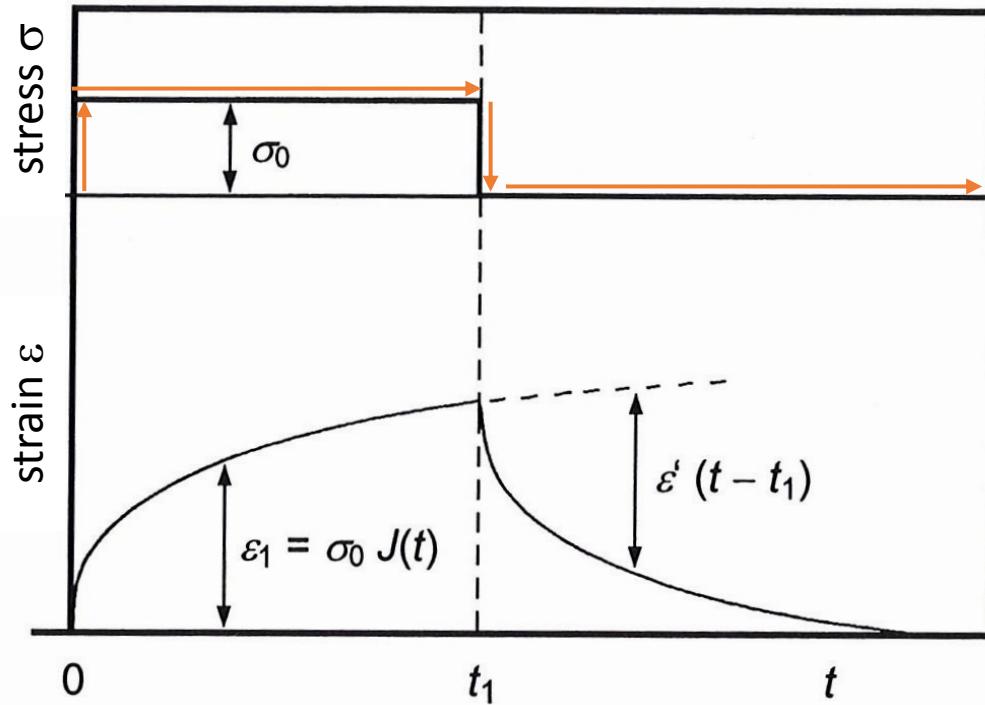
responding strain
 ε of the sample

$J(t)$: creep yield

$$\varepsilon(t) = \int_{-\infty}^t J(t - \tau) \Delta\sigma(\tau) d\tau$$

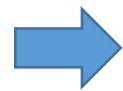
Boltzmann's superposition principle II

strain of a visco-elastic material under temporary tensile load



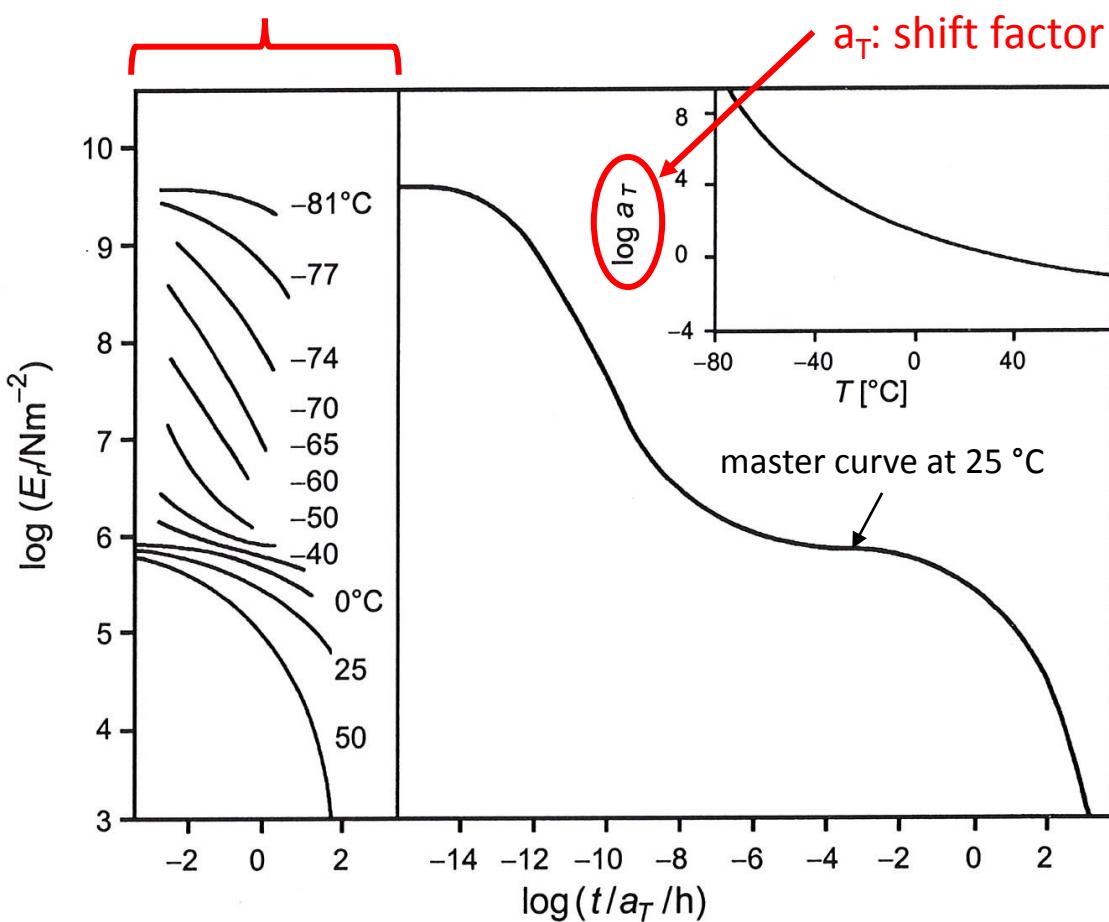
E_r : stress relaxation modulus

$$\sigma(t) = \int_{-\infty}^t E_r(t - \tau) d\varepsilon(\tau)$$



all the different deformation steps are separate

► Master curve from stress relaxation data



$$\log a_T = \log t - \log t_0 = \log \frac{t}{t_0}$$

Williams, Landel and Ferry

WLF equation

$$\log a_T = \frac{-c_1^g(T - T_g)}{c_2^g + (T - T_g)}$$

$$c_1^g = 17.4 \text{ K}$$

$$c_2^g = 51.6 \text{ K}$$

visco-elastic materials



time and temperature are equivalent

